

# A model for search and detection of small targets

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# Background

Navy wants models predicting target detection times on workstations.

Beau Watson and I have simple models for foveal target detection.

If targets could only be detected in the fovea and there are no other targets, the search model should also be simple.

# Summary

Search task: Target on horizon in uniform sky above a uniform ocean

Model: Random search with a saccade-distance penalty and inhibition-of-return with temporal decay

Lesson learned: Pre-detection information accumulation seems to be necessary.

# Stimuli

Screen distance: 69 cm      Image width: 38 cm

Image size in pixels: 1280 X 1024 (W X H)

Sky y pixel range: 0 – 509

Sky RGB color: 0 128 255  $\Rightarrow$  45.4 cd/m<sup>2</sup>

Target, ocean: 0 0 128  $\Rightarrow$  6.62 cd/m<sup>2</sup>

Target pixel size: 1 X 1

Target y position: 509

Target x positions:  $i \cdot 100$ ,  $i=1,12$

Blank screen fixation cross, x y: 512 384

(Samsung Syncmaster 910T LCD monitor)

# Methods

Eye positions recorded at 250 Hz by an SR Research Eyelink II head-mounted tracker.

The experiment was controlled by an SR Research Experiment Builder program.

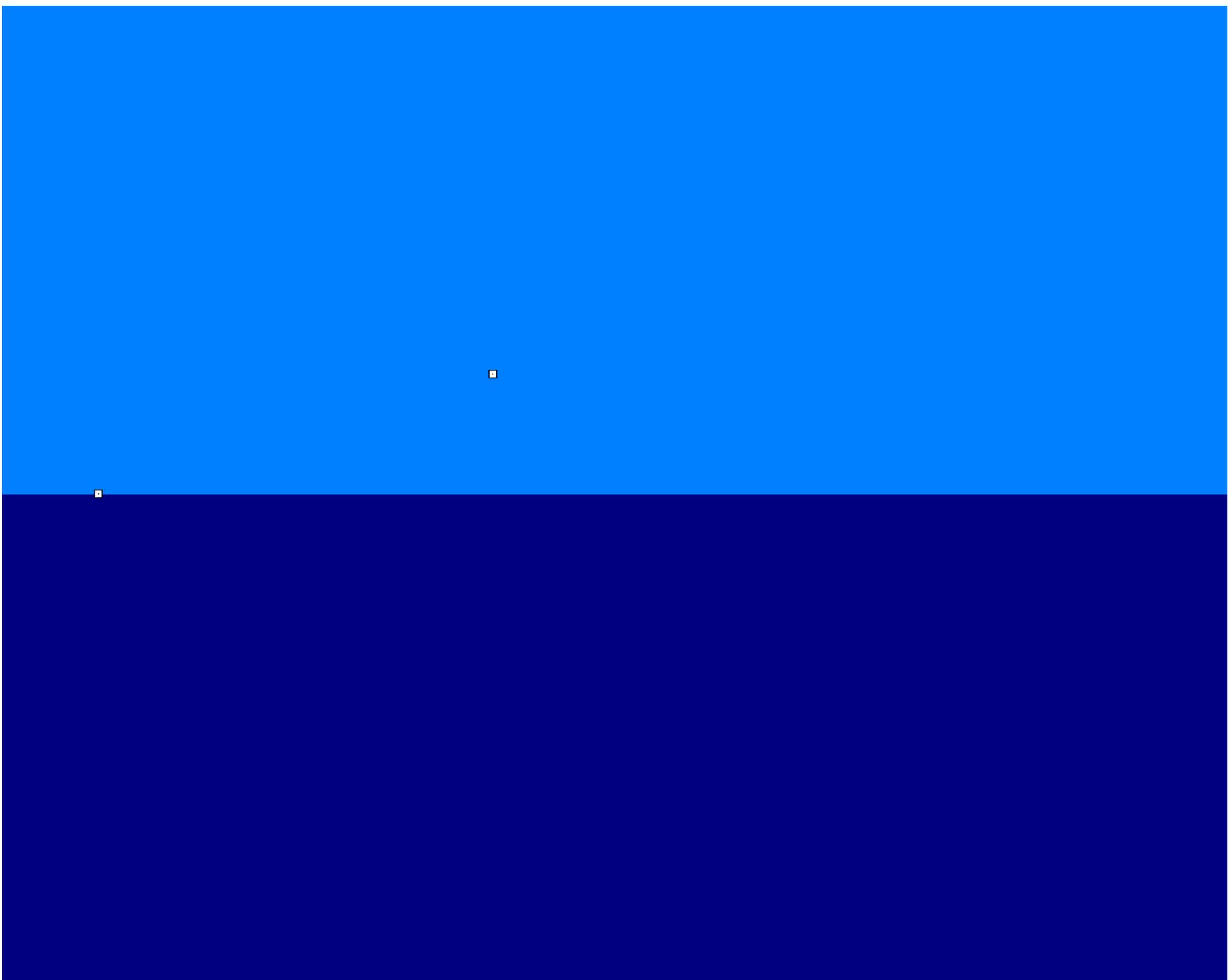
There were 3 test runs of 12 trials.

Before each 3 trial group a recalibration was performed.

Each test had all 12 positions in a random order.

The sequence of fixations was extracted by an SR Research Data Viewer program.

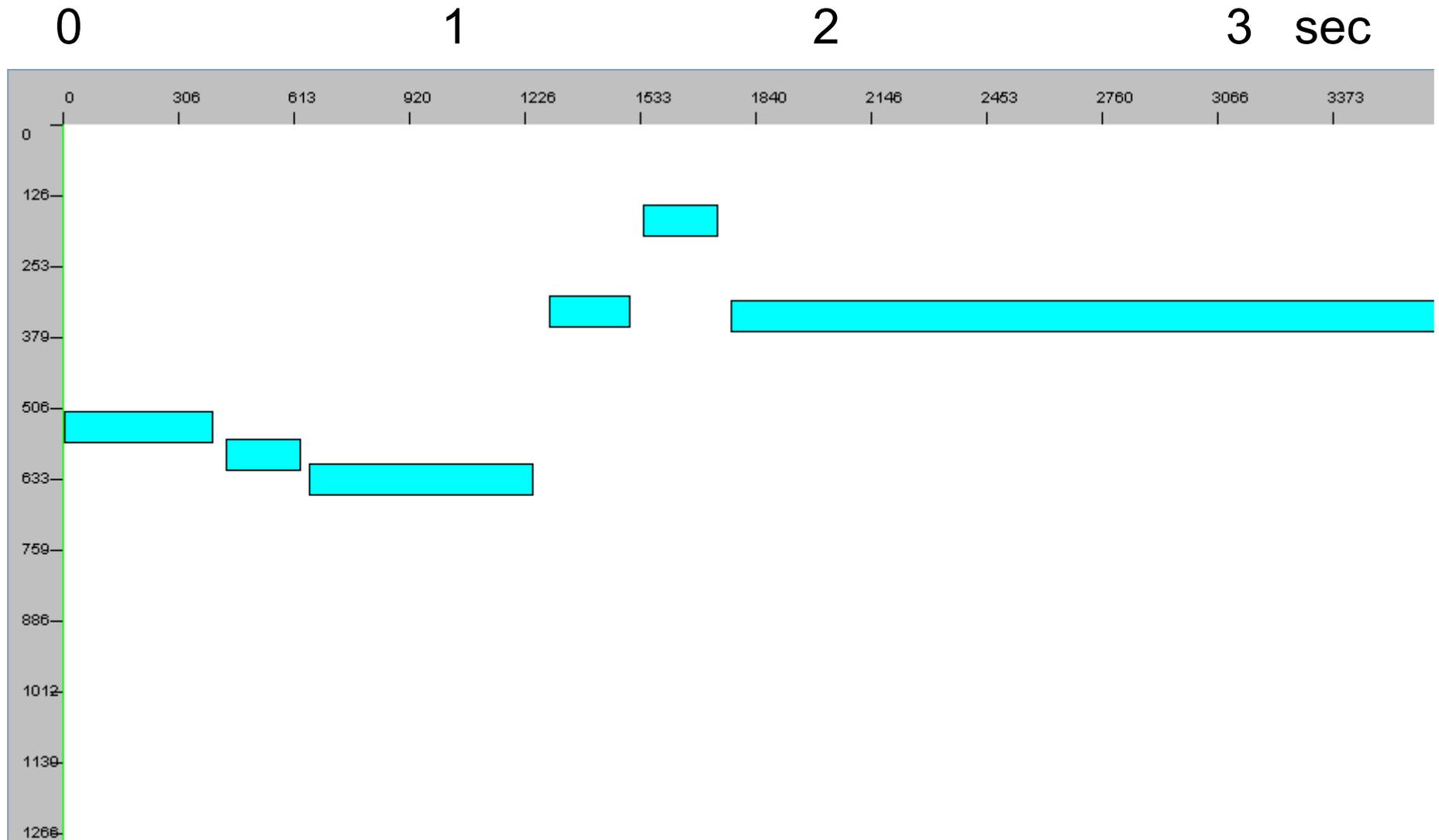
The data from the first test run was discarded.



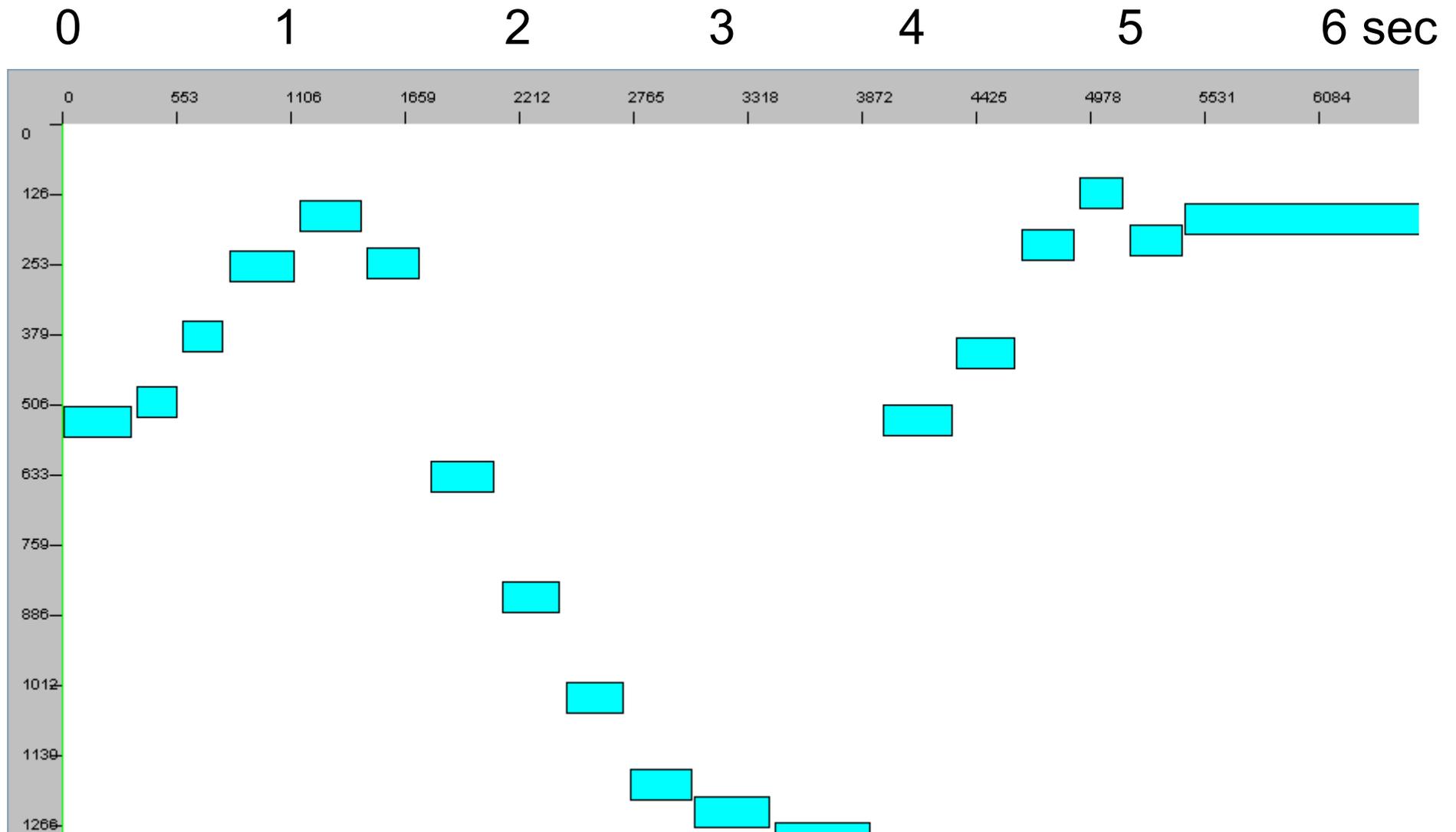
# Eyelink II



# Search data: Test 2 trial 1

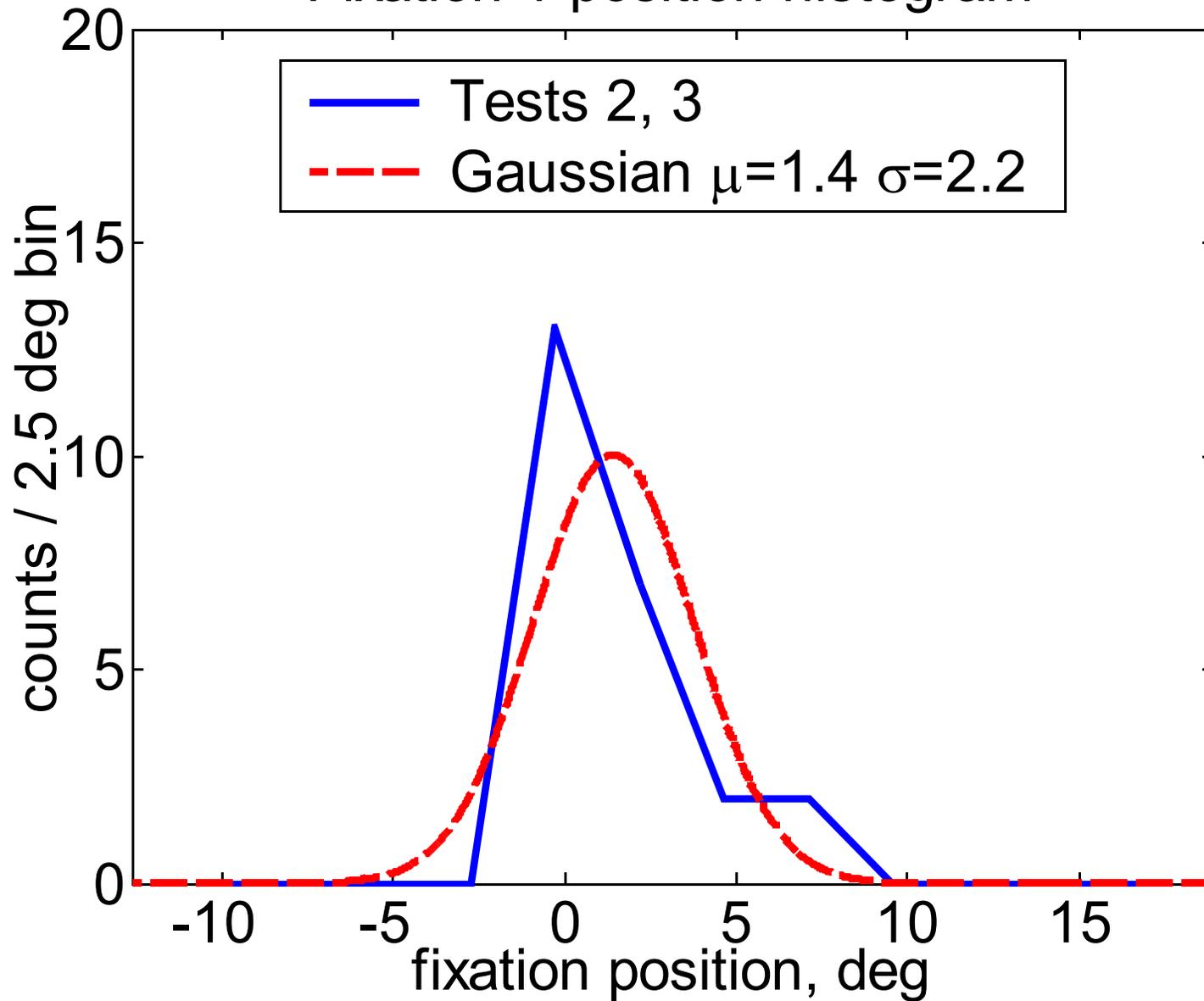


# Search data: Test 2 trial 2



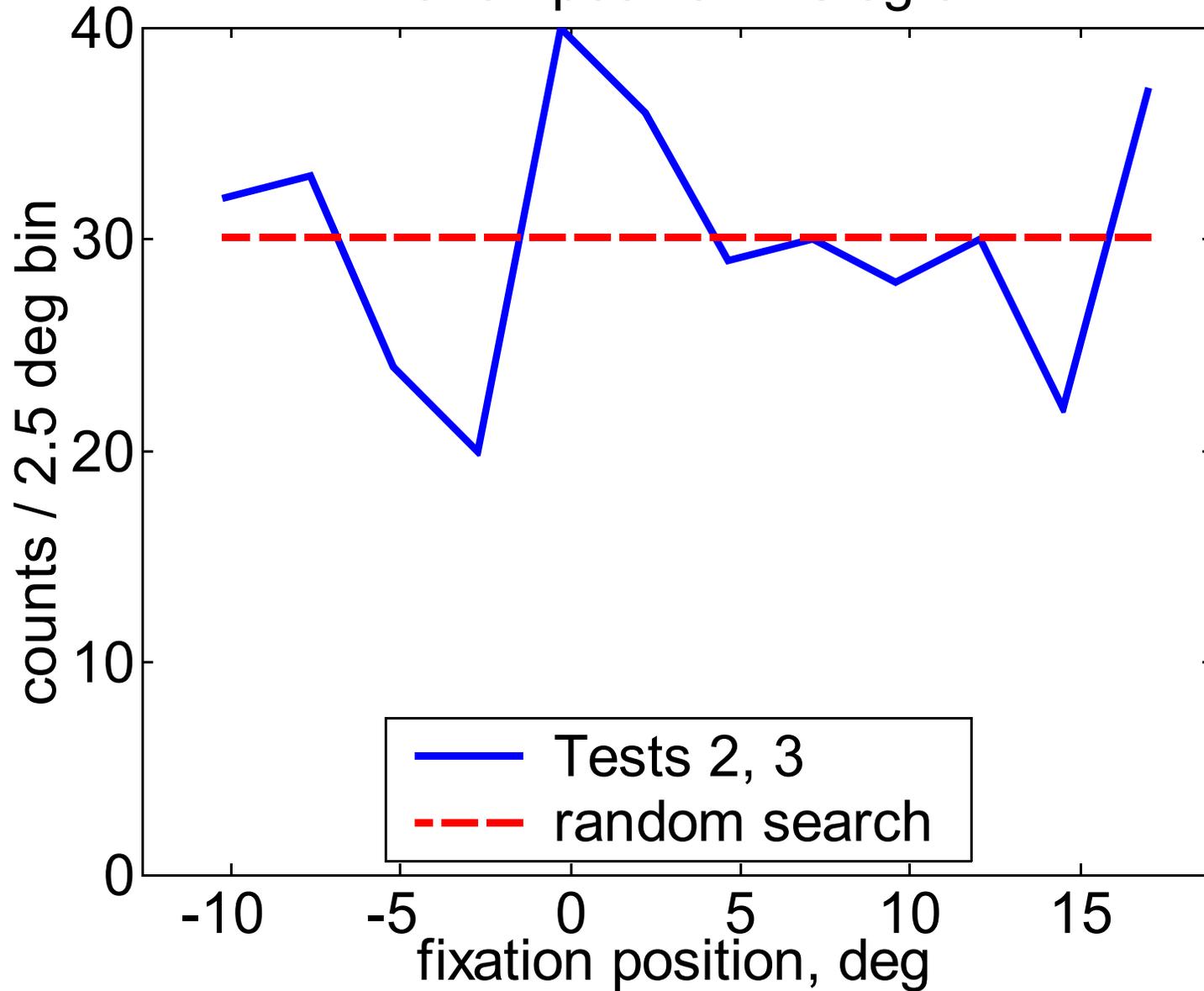
# Search data

Fixation 1 position histogram



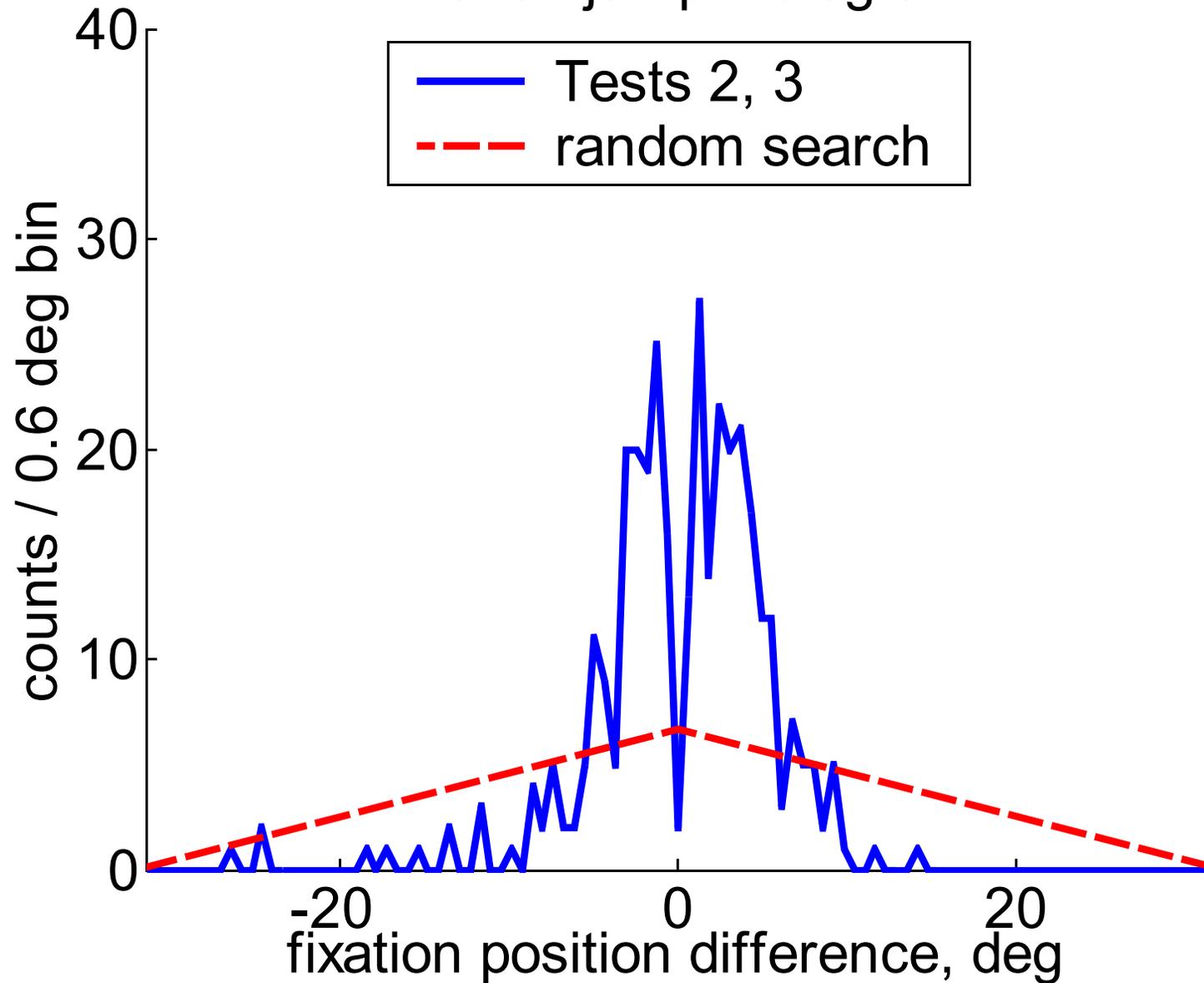
# Search data

Fixation position histogram



# Search data

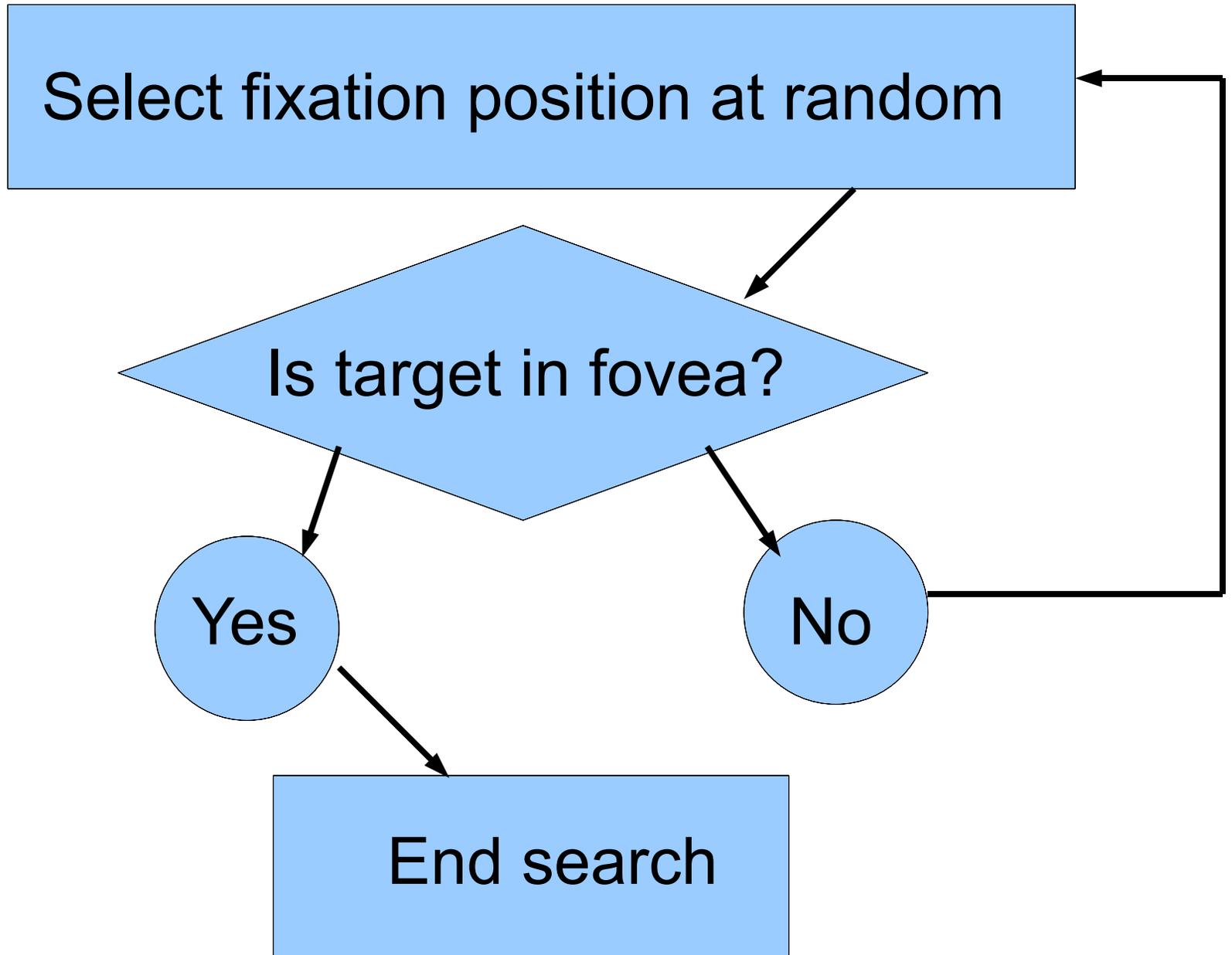
Fixation jump histogram



# Search data summary

	test 2	test 3	
median fixation duration	300	292	msec
mean fixations per trial	19.0	16.8	
standard deviation	9.4	10.2	

# Simplest Search Model



# Fixations

	mean	std dev	fovea, deg
test 2	19.0	9.4	
test 3	16.8	10.2	
simplest model	19	19	1.66

# Optimal Model

Divide horizon into fovea sized sections

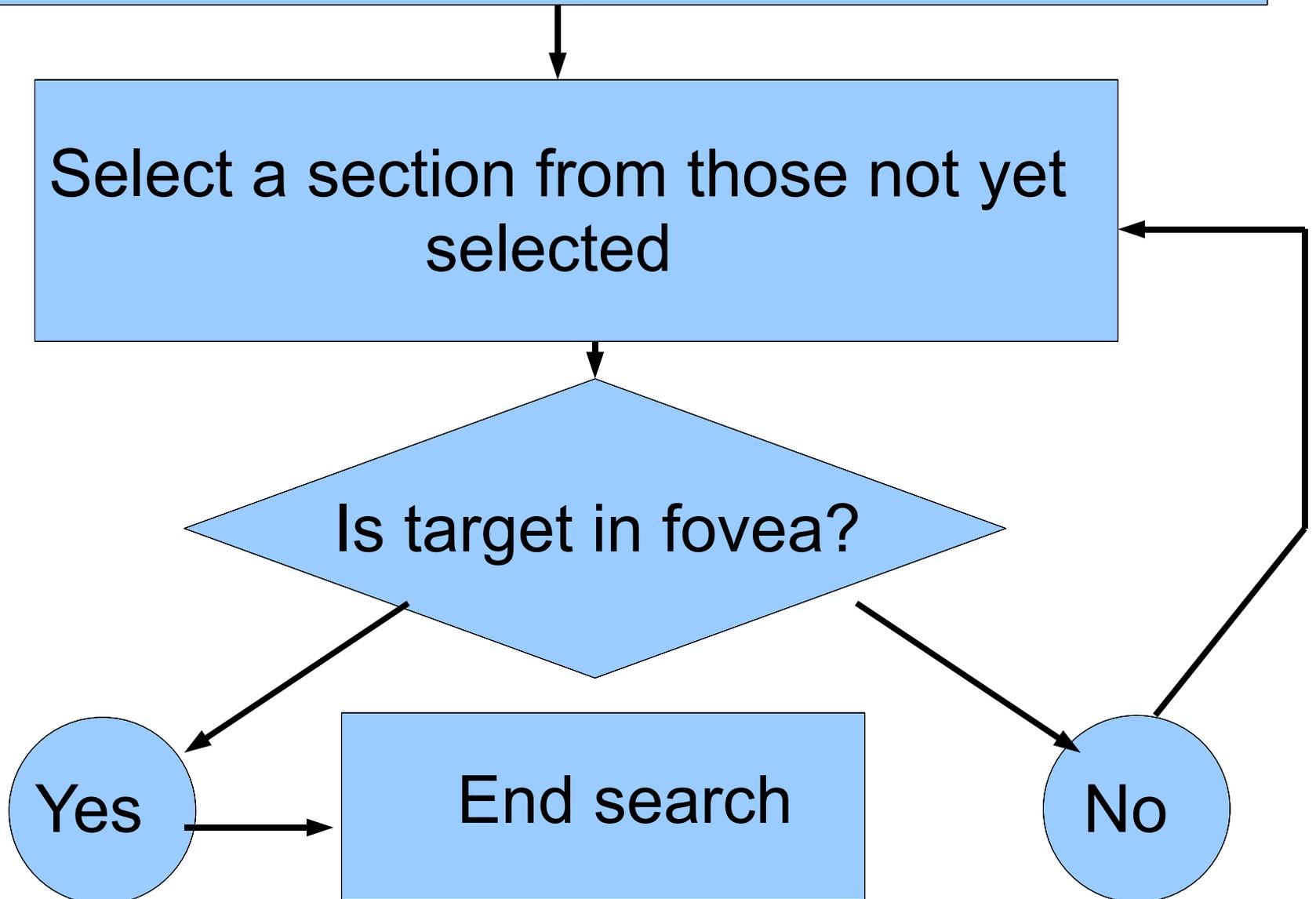
Select a section from those not yet selected

Is target in fovea?

Yes

End search

No



# Fixations

	mean	std dev	fovea, deg
test 2	19.0	9.4	
test 3	16.8	10.2	
simplest model	19	19	1.66
optimal model	19.0	9.7	0.13

# Simple Search Model

No saliency map

No expectancies

Distance penalty distribution

All-or-nothing fovea for detection and for inhibition-of-return with temporal decay

# Distance penalty function

Let  $D(x)$  be the probability density distribution of the position of next fixation given that the current fixation is at zero eccentricity and there is no Inhibition of Return.

Let  $x_0$  and  $x_1$  be the ends of the horizon and  $x_C$  be the center of fixation

The the un-normalized distance penalty is  
 $D(x-x_C)$ ,  $x_0 < x < x_1$

# Inhibition of return function

$H(n, x)$  is Inhibition on fixation  $n$  at position  $x$

$$H(1, x) = 0$$

$F(n, x) = 1$  if  $x$  is in the fovea on trial  $n$ ,  
 $= 0$  otherwise

Update rule:

$$H(n, x) = \min(1, h H(n-1, x) + R(n, x))$$

Usage: unnormalized distribution is

$$(1-H(n, x)) D(x-x_C)$$

# Distance and Inhibition Model

Select fixation on horizon near fixation mark

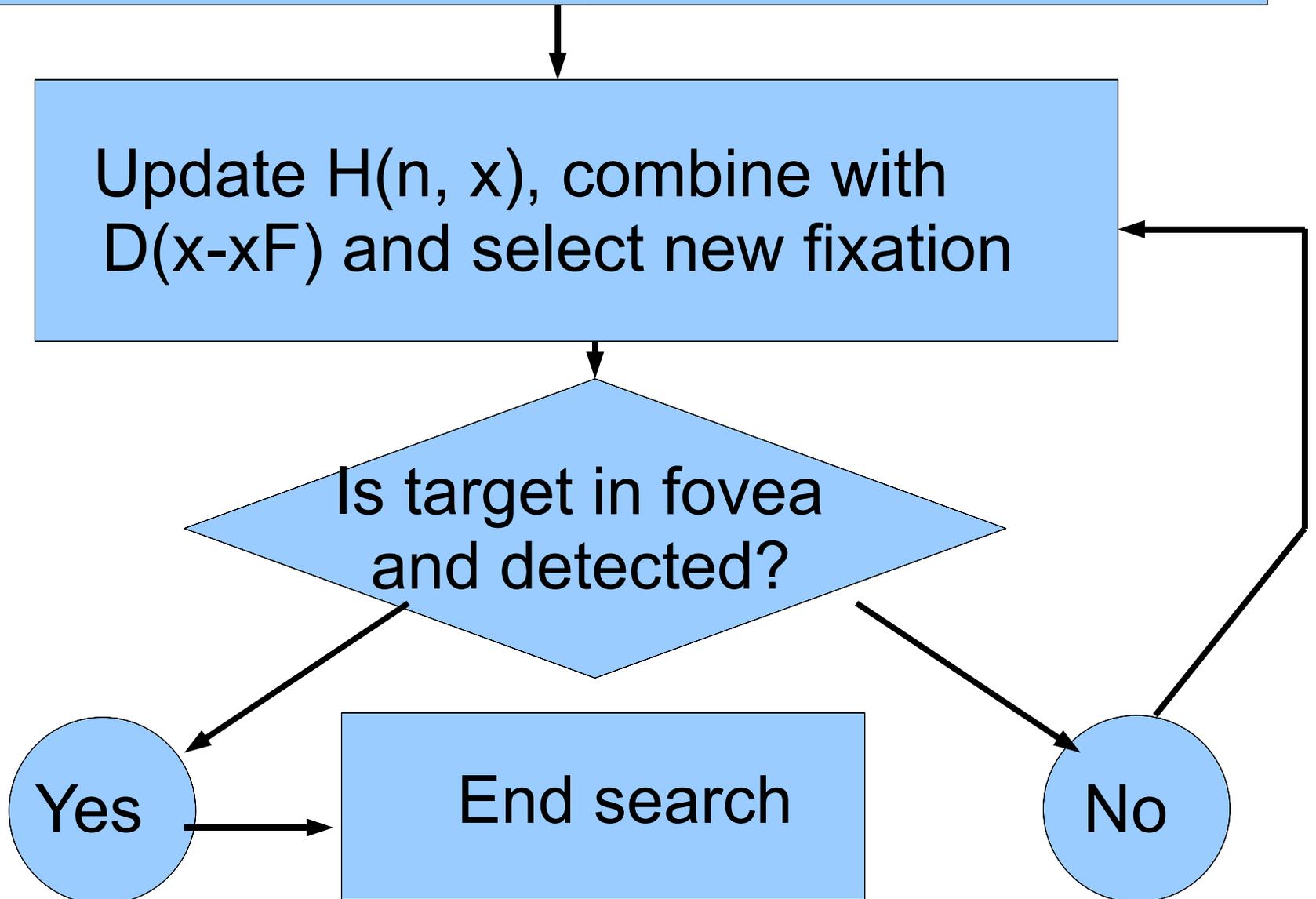
Update  $H(n, x)$ , combine with  $D(x-x_F)$  and select new fixation

Is target in fovea  
and detected?

Yes

End search

No



# Fixations

	ave	std	std/ave fovea,	
deg				
test 2	19.0	9.4	0.49	
test 3	16.8	10.2	0.61	
simplest model	19	17.2	0.90	1.66
optimal model	19.0	9.7	0.50	0.13
inhib & dist	18.2	13.3	0.73	1.02

# Evidence function

$E(n, x)$  is target evidence on trial  $n$  for position  $x$

$$E(1, x) = 0$$

Update rule:

$$\begin{aligned} E(n, x) &= e + E(n-1, x) \text{ if } x \text{ is in perifovea on trial } n, \\ &= E(n-1, x) \text{ otherwise} \end{aligned}$$

Usage: unnormalized scan distribution is

$$(1-H(n, x)) D(x-x_C) + E(n, x)$$

# Fixations

	ave	std	std/ave fovea,	
deg				
test 2	19.0	9.4	0.49	
test 3	16.8	10.2	0.61	
simplest model	19	17.2	0.90	1.66
optimal model	19.0	9.7	0.50	0.13
inhib & dist	18.2	13.3	0.73	1.02
inhib & dist & evid	19.6	12.4	0.63	0.97

# Parameters

initial distribution:  $m = 1$  deg,  $s = 2$  deg

distance penalty distribution:  $m = 0$ ,  $s = 5$  deg

inhibition persistence factor:  $h = 0.99$

evidence per fixation:  $e = 0.2$

foveal width: 1 deg

perifoveal width: 3 deg

# Detection computation

Filter signal on horizon image  $S(x,y)$  with low pass (optical) filter  $V(x,y) = S(x,y) * O(x,y)$ .

Form local luminance image  $L(x,y)$  by filtering with surround filter  $L(x,y) = V(x,y) * B(x,y)$ .

Compute contrast image  $C(x,y) = V(x,y) ./ L(x,y) - 1$

Compute masked contrast image

$$M(x,y) = C(x,y) / (1 + k B(x,y) * (C(x,y).^2)).^0.5$$

Subtract no-signal masked contrast image and compute contrast energy.

# Shortcut computation

Ocean luminance =  $6.62 \text{ cd/m}^2$

Sky luminance =  $45.4 \text{ cd/m}^2$

Local luminance at target =  $26.0 \text{ cd/m}^2$

Signal contrast =  $6.62/26.0 - 1 = -0.75$

Signal duration =  $0.3 \text{ sec}$

Pixel width =  $0.025 \text{ deg}$

Contrast energy =  $\text{width}^2 \text{ duration contrast}^2$

dBB =  $60 + 10 \log_{10}(\text{energy}) = 20$

Gaussian low pass  $\exp(-(\text{f}/15 \text{ cpd})^2)$

attenuation =  $-7 \text{ dB}$

RMS contrast at target is signal contrast

Masking factor =  $1/\sqrt{1+(-0.75/0.6)^2} \Rightarrow -4 \text{ dB}$

Effective signal energy =  $9 \text{ dBB}$

# Sensitivity comparison

Thresholds of 16 Modelfest observers  
mean = 7 dBB, std dev = 2 dB

Modelfest threshold was 84% correct in  
2 interval forced choice.

2IFC has a  $d'$  of root 2 larger than Y/N, i. e.  
a 3 dB improvement, so the predicted  
Y/N threshold for the Modelfest observers  
is 10 dBB

The difference between an 84% and a 75% 2IFC  
contrast threshold is about 2 dB \*

$$(z((.84-0.5)/0.5) - z((.75-0.5)/0.5) ) = 1 \text{ dB}$$

**Next Step**

**Collect more data!**

# Suggestion

Eye position recorders are usually calibrated with a simple “follow the spot” procedure. Perhaps a short “horizon” search and detection would help calibrate the distance penalty, inhibition, and detection parameters before expectations and stimulus attractors are included.